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## Electron Environment at Geostationary Orbit: AE9 Summary Results

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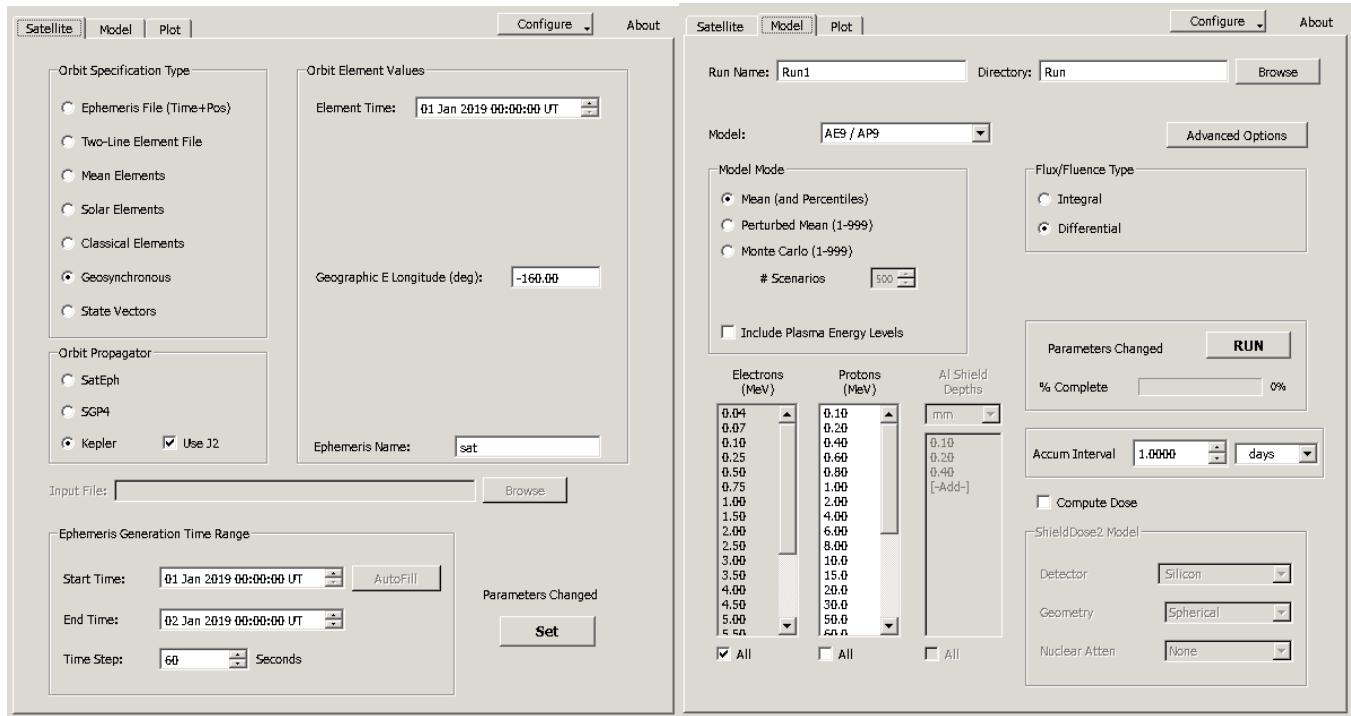
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## 1. Introduction

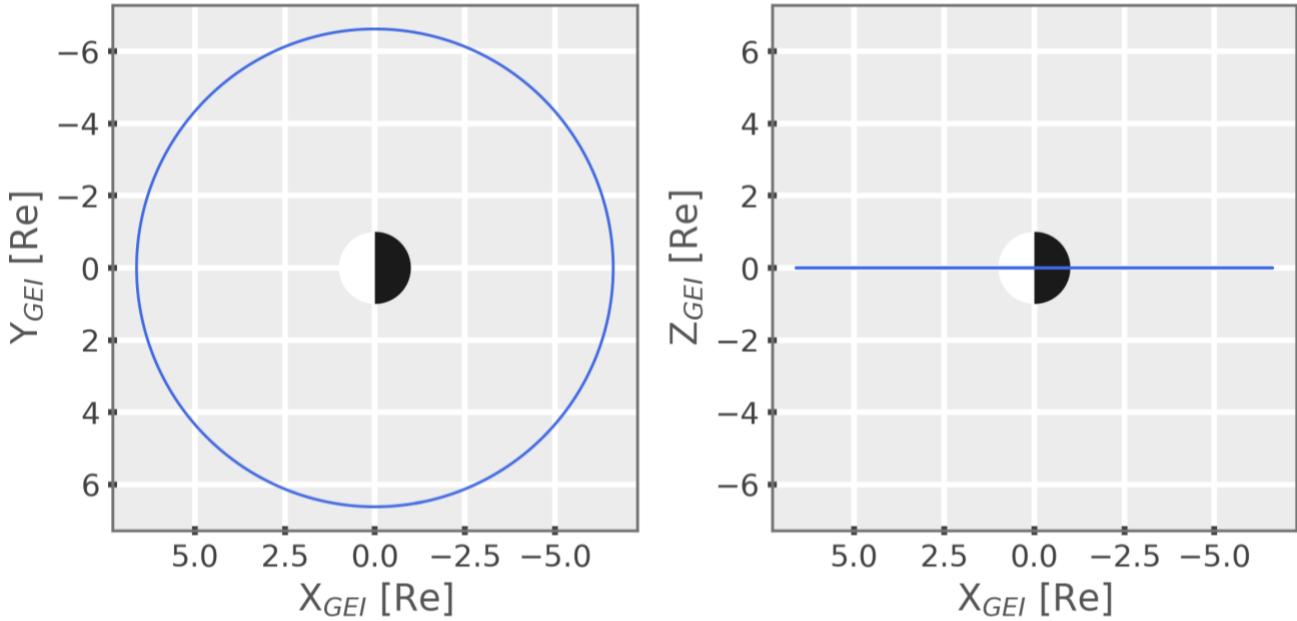
This report captures the outputs from the AE9 for the electron environment at geostationary orbit. There is no new work, simply a collection of model outputs to make them easier to use and tailored to quick data gathering for geostationary orbit studies. Other models do exist, such as POLE [1], but a comprehensive look at each is beyond the scope of this work. Other resources are contained in the references.

## 2. Model and Setup

The model utilized is the AE9 model version 1.50.001 [2-5]. AE9/AP9 is the new community standard trapped radiation specification model following after the AE8/AP8 model [6]. For this work, the model was run on OSX through wine [7] and analyzed using the ae9ap9 module in SpacePy [8], pandas [9], matplotlib [10], jupyter notebooks [11], and SciPy [12], all in python 3.7 [13]. The model parameters are shown in Figure 1. The variation as a function of time was found to be minimal after a yearly run with 60 second resolution so one day was run for all the cases. Ephemeris was computed in geocentric equatorial inertial (GEI) coordinates [14] and reported fluxes are omnidirectional and differential in energy. In GEI coordinates geostationary orbit forms a circle at 6.6 Earth radii ( $R_E$ ) as shown in Figure 2. Identical model runs were performed for longitudes every 20 degrees around the globe. Percentile fluxes every 5% from 5% to 95% were tabulated. For the AE9 model percentiles are the fraction of the data below a given flux value over all time. This intentionally does not have a solar cycle or other dependence in order to give these percentiles the intended meaning.



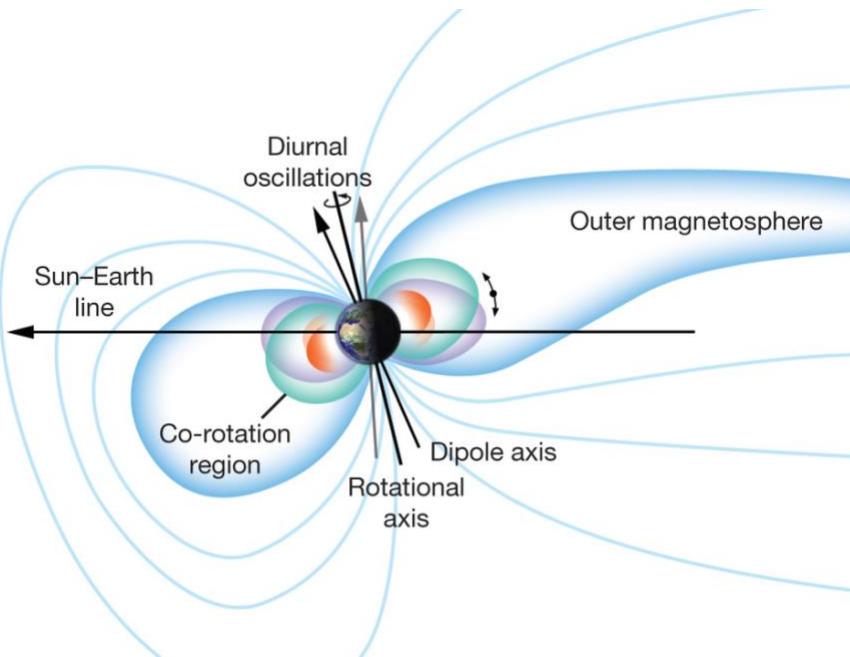
*Figure 1 Screenshots of the AE9 model parameters.*



*Figure 2 Plot of a one-day orbit track in geostationary orbit in GEI coordinates.*

### 3. Overview

The energetic ( $\sim$ MeV) trapped electron population is known as the Van Allen Radiation belt [15]. These electrons are trapped on magnetic field lines and the magnetic field is not aligned with Earth's spin axis. Figure 3 shows a schematic view of Earth's magnetosphere. The trapped electron population is in the Co-rotation region noted in the figure.



*Figure 3 Schematic view of Earth's magnetosphere, from [16].*

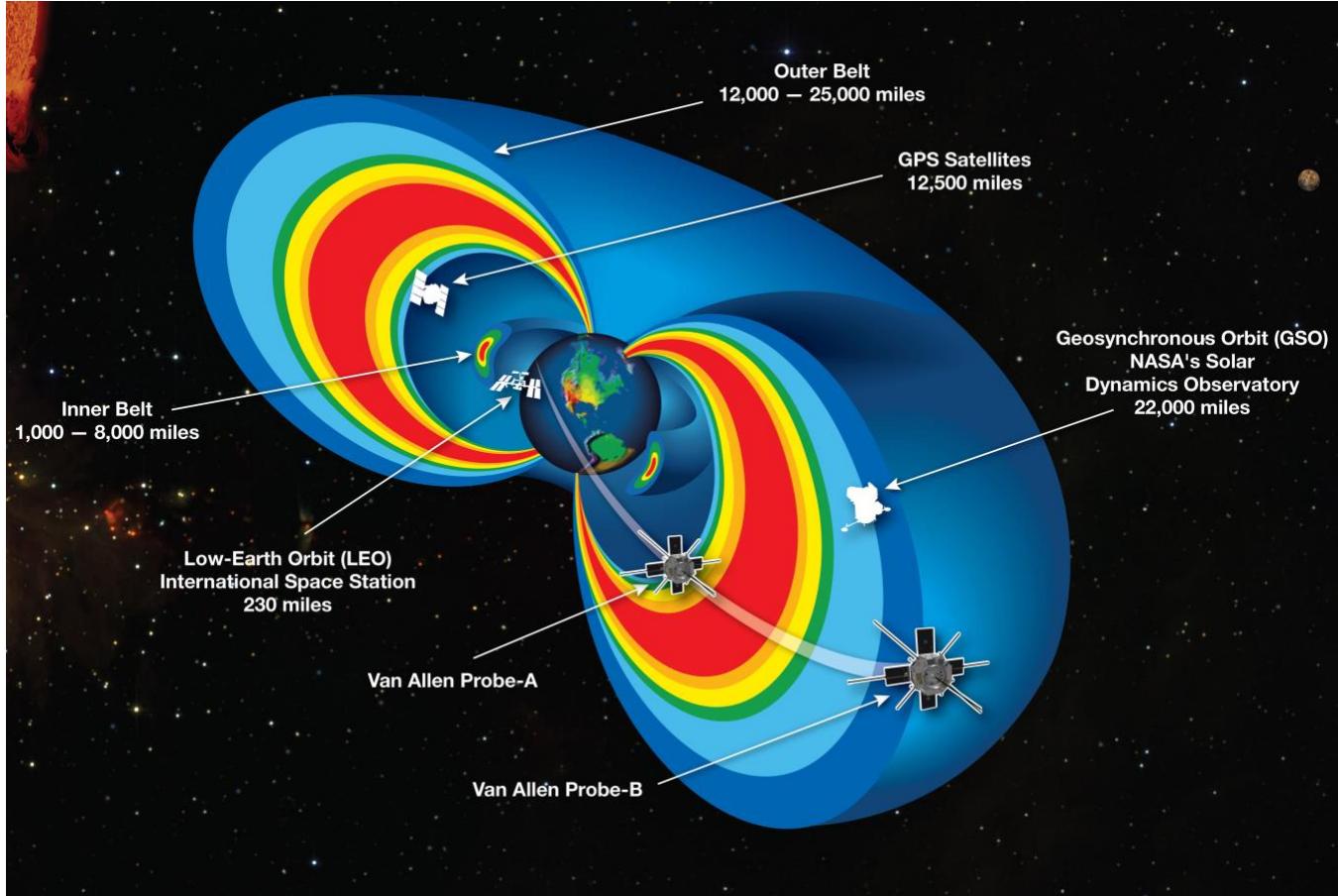


Figure 4 Figure showing the notional radiation belt intensity as a function of location around the Earth. Several orbits are denoted with their position relative to the notional maximum. From NASA.

#### 4. Results and Narrative

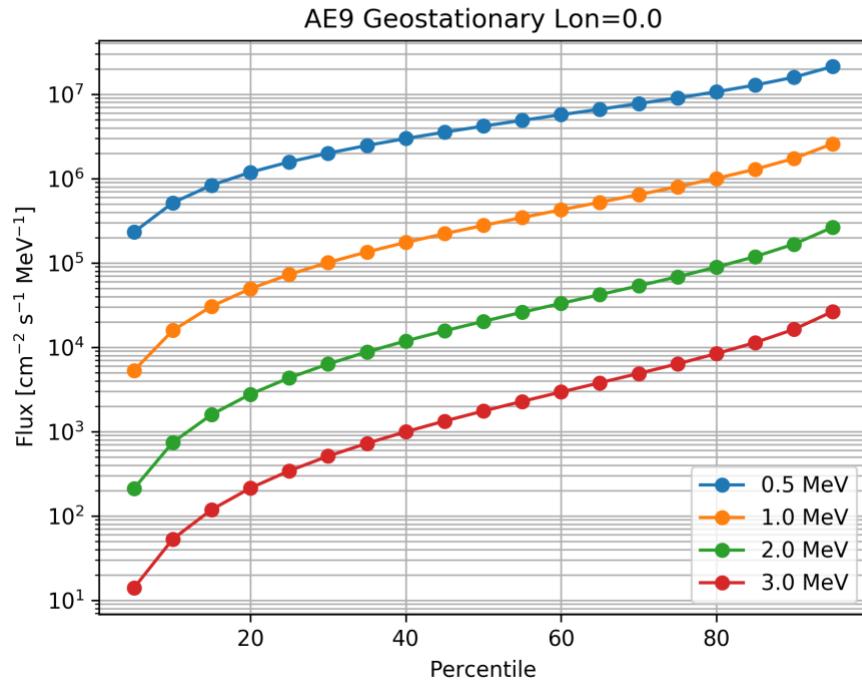
This section contains model output results and a narrative on how to utilize these outputs for follow-on studies.

**The electron radiation belt has a huge variation in intensity.** Figure 5 shows the difference with energy and with percentile. For the same energy, 1 MeV as an example, there is a factor of 489 between 95<sup>th</sup> and 5<sup>th</sup> percentile. Figure 6 shows the ratios between 95<sup>th</sup>/5<sup>th</sup> and 95<sup>th</sup>/50<sup>th</sup> as a function of energy for 0° longitude.

**The electron radiation belt has a strong energy dependence.** Figure 9 shows the energy spectra as a function of percentile. In the AE9 model there is little dependence on percentile for the spectral shape.

**The electron radiation belt has a slight dependence on longitude.** Figure 10 shows the ratio compared to 0° longitude for several energies and percentiles.

As the fluxes as a very steep function of energy and percentile, special care must be taken in interpolation. Good choices are BSpline and Piecewise Cubic Hermite Interpolating Polynomial (PCHIP) both part of scipy interpolate.



*Figure 5 Radiation belt fluxes are a falling spectrum with roughly an order of magnitude between each of the presented energies.*

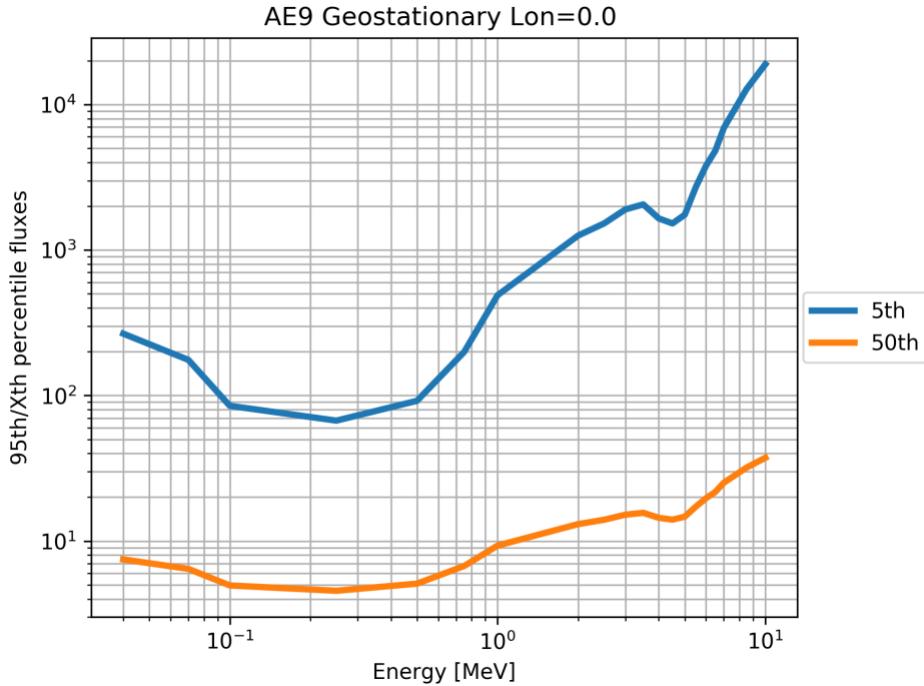


Figure 6 Flux ratios between 95<sup>th</sup> and 5<sup>th</sup> and 50<sup>th</sup> percentiles for 0° longitude.

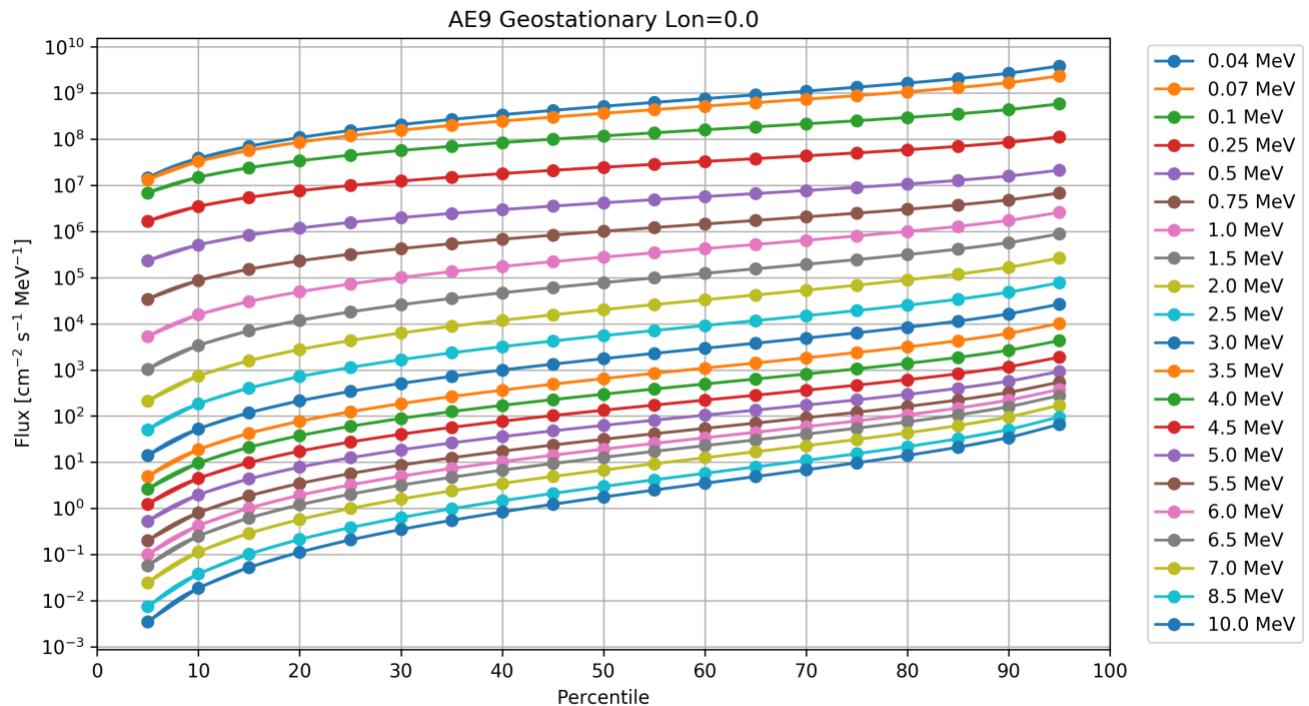
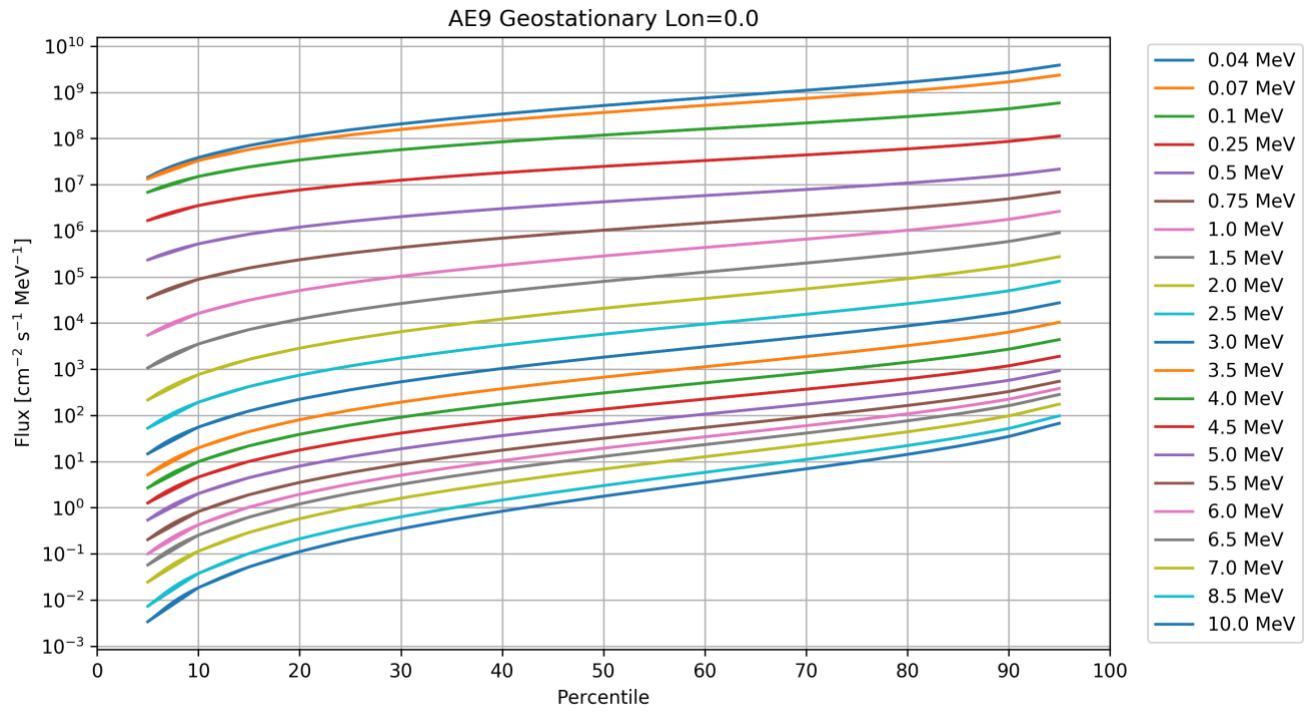
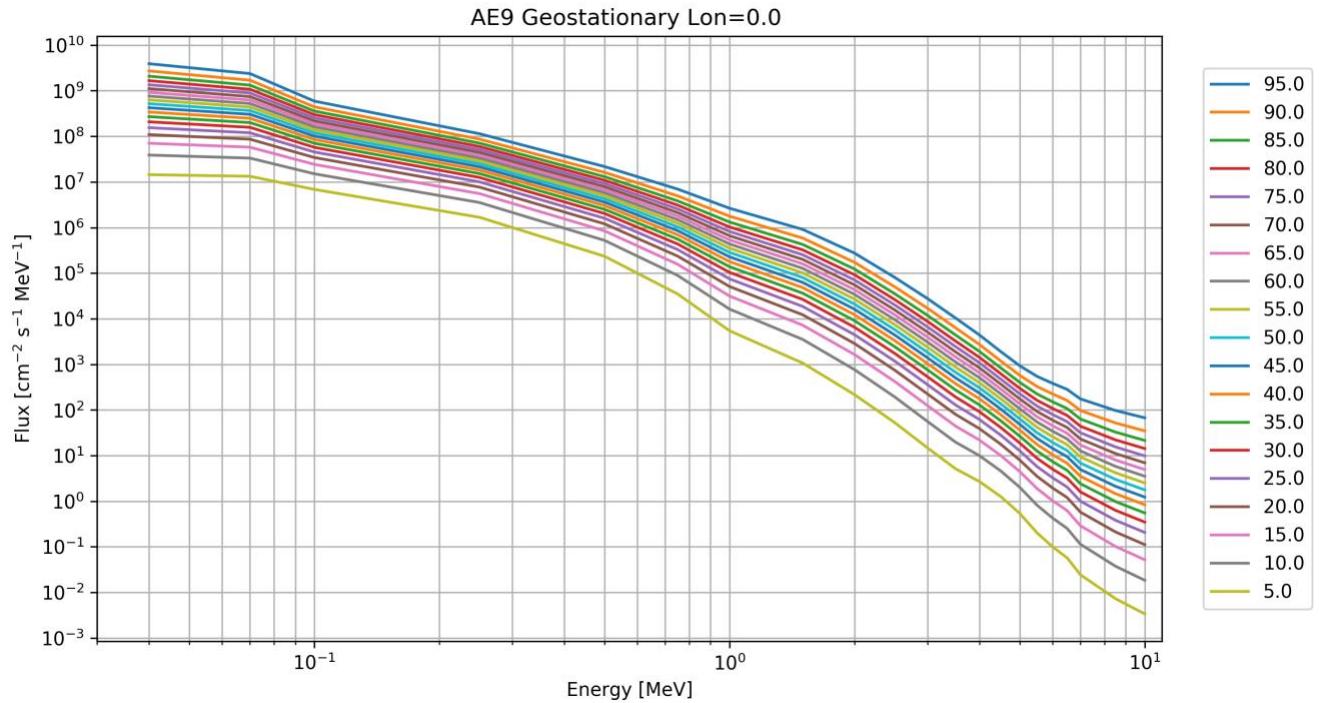


Figure 7 All computed fluxes and a function of percentile at 0° longitude.

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*Figure 8 All computed fluxes and a function of percentile at  $0^\circ$  longitude. This is the same as Figure 7 without the points drawn.*



*Figure 9 All computed fluxes as a function of energy for various percentiles at  $0^\circ$  longitude.*

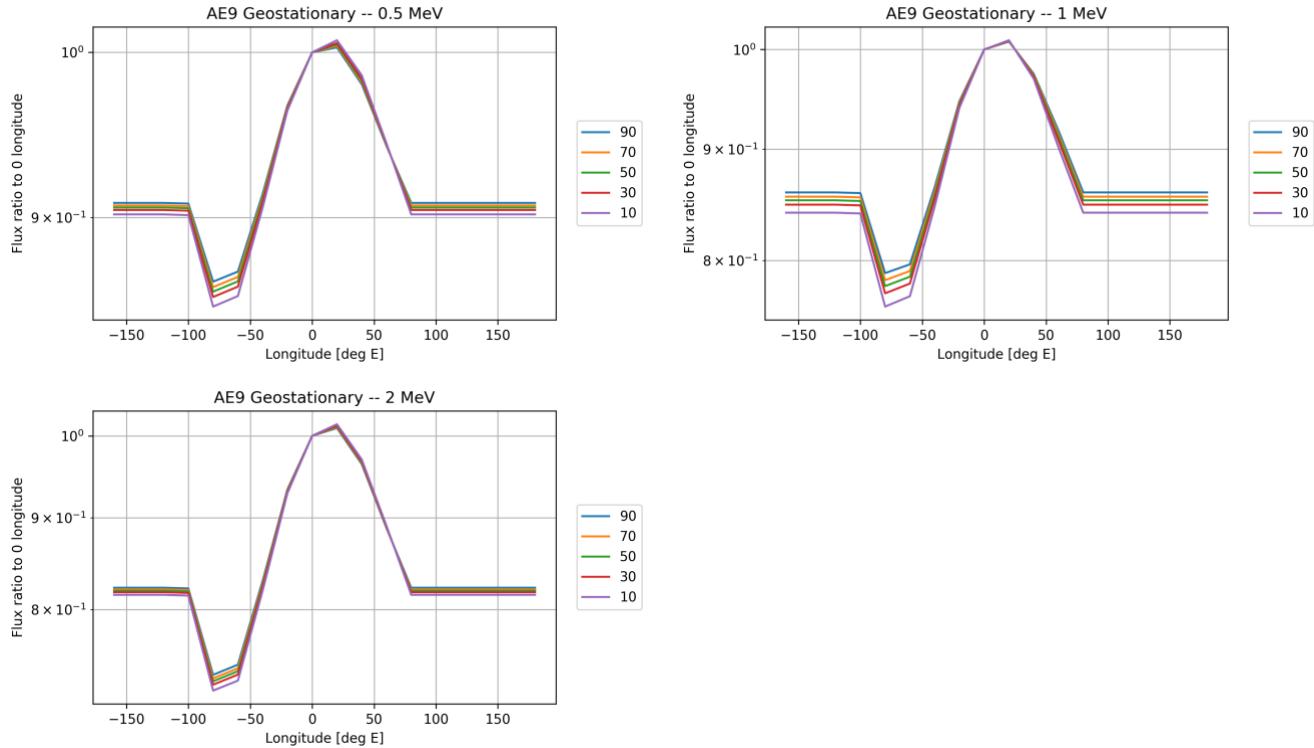


Figure 10 Flux ratios as a function of longitude and percentile compared to the value at  $0^\circ$ .

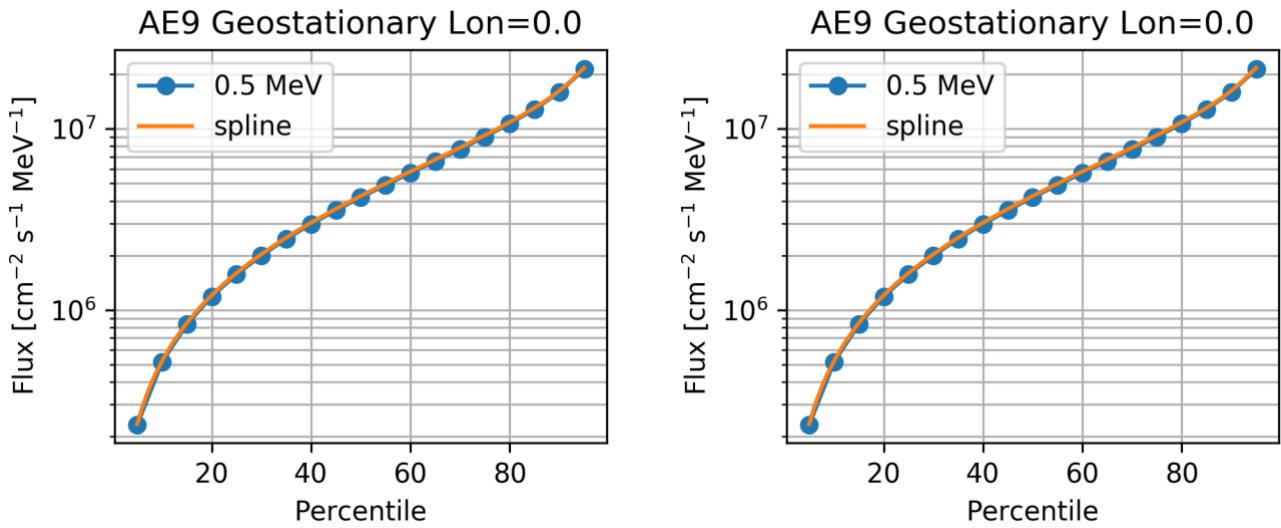


Figure 11 Example interpolations in percentile space, left is BSpline and right is PCHIP.

## 5. Other Resources

Textbooks: [14, 17-19]

Presentations: [20]

This work, code, and data are cataloged for LANL use at: <https://git.lanl.gov/SABRS-NGP/geo-swx-percentiles>

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## 7. Appendix: Tabulated Spectra

This appendix contains tabulated spectra for 0° longitude. Column header are percentile fluxes, the rows are energies (MeV), and the values of the omnidirectional differential electron number flux ( $\text{cm}^{-2}\text{s}^{-1}\text{MeV}^{-1}$ ).

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	<b>95</b>	<b>90</b>	<b>85</b>	<b>80</b>	<b>75</b>	<b>70</b>	<b>65</b>	<b>60</b>	<b>55</b>	<b>50</b>	<b>45</b>	<b>40</b>	<b>35</b>	<b>30</b>	<b>25</b>	<b>20</b>	<b>15</b>	<b>10</b>	<b>5</b>
<b>0.04</b>	3.85E+09	2.68E+09	2.05E+09	1.64E+09	1.34E+09	1.1E+09	9.11E+08	7.56E+08	6.26E+08	5.15E+08	4.21E+08	3.39E+08	2.68E+08	2.07E+08	1.54E+08	1.09E+08	70385059	38842932	14478536
<b>0.07</b>	2.34E+09	1.67E+09	1.31E+09	1.06E+09	8.78E+08	7.34E+08	6.17E+08	5.19E+08	4.39E+08	3.64E+08	3.01E+08	2.47E+08	1.99E+08	1.56E+08	1.19E+08	86176173	57610569	33225158	13323047
<b>0.1</b>	5.82E+08	4.37E+08	3.53E+08	2.95E+08	2.51E+08	2.15E+08	1.85E+08	1.6E+08	1.37E+08	1.18E+08	1E+08	84295341	69980799	56945051	45032124	34128115	24142577	15043587	6858711
<b>0.25</b>	1.12E+08	85282875	69791522	58869743	50448899	43596552	37834170	32866552	28505712	24623757	21129757	17956860	15054616	13384200	9915344	7624401	5493242	3509167	1667304
<b>0.5</b>	21276253	15876615	12799409	10659962	9026621	7719150	6628364	5697874	4888636	4177872	3544357	2975797	2462262	1996324	1572011	118369	833440	514947.9	231490.8
<b>0.75</b>	6790646	4819578	3744763	3022691	2488685	2071167	1732723	1451423	1213360	1009202	832417.7	678291	543341.8	424974.5	321262.9	230829	1528097	86953.44	34096.1
<b>1</b>	2833264	1779618	1287476	1002073	798236.9	6439157	522616.4	424798.9	344484.2	277699.9	221689.1	174473.6	134599.1	100579.3	72799.26	494559.98	30329.7	15790.05	5284.258
<b>1.5</b>	8833378	570676.9	413756.8	314919.2	248823.5	194336	154978	123664.3	98426.75	77834.56	60899.79	46916.33	33365.96	25880.87	18107.62	11884.31	7027.262	3426.848	1040.06
<b>2</b>	264684.9	166725	118652.3	88893.2	68401.21	53401.55	41985.88	33067.06	25972.69	20261.14	15628.77	11859.27	8794.144	6314.743	4330.922	2773.711	1590.745	743.9685	210.6409
<b>2.5</b>	77288.93	48090.12	33915.65	25214.53	19366.83	14942.72	11673.13	9134.933	7128.836	5524.275	4231.678	3187.335	2344.624	1668.653	1132.869	716.8725	405.0044	185.5591	50.76904
<b>3</b>	26555.83	16287.21	11365.57	8374.102	6366.818	4884.516	3787.383	2941.928	2278.686	1752.22	1331.443	994.2919	724.6467	510.4504	3425.192	213.769	118.7073	53.12242	13.97798
<b>3.5</b>	10104.21	6162.849	4283.233	3145.144	23756.435	1823.983	1410.1	1092.32	843.7791	646.9656	490.1638	364.9108	265.0642	186.0314	124.3141	77.21051	42.62019	18.92012	4.913893
<b>4</b>	4292.683	2655.582	1865.034	1318.1697	1052.455	813.8458	633.9678	494.7348	385.0085	297.5013	227.2188	170.6123	125.0864	88.69936	59.97314	37.77035	21.21471	9.644599	2.606187
<b>4.5</b>	1875.781	1166.509	822.4049	611.2623	466.9826	362.1171	282.8445	221.3178	172.6987	133.8177	102.5009	77.20218	56.79024	40.41851	27.744286	17.36837	9.815206	4.49941	1.232591
<b>5</b>	920.5557	567.9645	397.9764	294.253	223.7235	172.6951	134.2899	104.6115	81.26179	62.67264	47.76992	35.7907	26.17712	18.51183	12.471701	7.8277853	4.375206	1.97531	0.52737
<b>5.5</b>	540.4868	323.9549	222.2693	161.4312	120.7658	91.80592	70.33713	53.99088	41.311981	31.38348	23.54138	17.34072	12.4517	8.628063	5.682187	3.468764	1.87386	0.807593	0.19965
<b>6</b>	376.392	220.1154	148.3446	106.1315	78.32901	58.79335	44.49915	33.74926	25.51912	19.14575	14.18011	10.30634	7.205321	4.976569	3.220414	1.963559	1.015188	0.423456	0.099469
<b>6.5</b>	276.7518	158.813	105.5755	74.67242	54.54836	40.55204	30.41344	22.82966	17.13059	12.73585	9.344791	6.725849	4.711686	3.17819	2.031209	1.197868	0.620679	0.223366	0.057664
<b>7</b>	170.5228	95.21289	62.04848	43.15838	31.05676	22.76698	16.8438	12.49265	9.237601	6.775081	4.901837	3.476442	2.397329	1.589385	0.996657	0.574935	0.290074	0.114371	0.024689
<b>8.5</b>	95.09678	50.83047	32.07579	21.71683	15.25195	10.92848	7.909026	5.739789	4.152577	2.978463	2.105702	1.457442	0.97911	0.630892	0.383044	0.212856	0.102599	0.038076	0.00747
<b>10</b>	65.65681	34.08782	21.06634	14.01218	9.684978	6.836447	4.876678	3.489161	2.488564	1.759178	1.22512	0.834637	0.551287	0.348708	0.207373	0.112503	0.052669	0.018809	0.003475

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